

A Segment-Swapping Approach for Executing Trapped Computations

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Logic programming and parallelism

- (C)LP is a very interesting framework for parallelism:
 - ▶ Program closer to problem.
 - ▶ Notion of control provides more flexibility.
 - ▶ *Central parallelization challenges still there:*
 - ★ dependencies, heap, pointers, aliasing, ...but cleaner semantic setting (e.g., pointers exist, but are declarative).
- Two main types of parallelism:
 - ▶ *Or-Parallelism*: explore in parallel **alternative search paths**.
 - ▶ *And-Parallelism*: execute in parallel **parts of each execution path** (statements, procedure calls, ...)
 - ★ Traditional parallelism: parbegin-parend, loop parallelization, divide-and-conquer, etc.

Background: parallel execution and independence

- **Correctness:** same results as sequential execution.
- **Efficiency:** ideal execution time \leq than seq. program (no slowdown).

<pre>main :- s1 p(X), s2 q(X), write(X).</pre>	<pre>p(X) :- X = [1,2,3]. q(X) :- X = [], large computation. q(X) :- X = [1,2,3].</pre>
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- Fundamental issue: p *affects* q (prunes its choices).
 - ▶ q ahead of p is *speculative* \rightarrow **not independent**.

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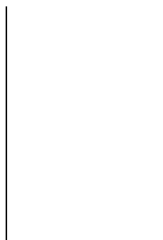
- Fundamental issue: p *affects* q (prunes its choices).
 - ▶ q ahead of p is *speculative* \rightarrow **not independent**.
- We will focus herein on **independent** and-parallelism (IAP).
 - ▶ Many interesting issues in parallelization: dependency analysis (pointer sharing, determinacy, non-failure, ...), granularity/ovhd. analysis, ...
 we assume program parallelized (using $\&/2$: simple fork-join, nested).

IAP: deterministic example

```
m :- a(X) & a(Y).
```

```
a(1).
```

GOALS



IAP: deterministic example

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GOALS

m

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GOALS

a(X)

a(Y)

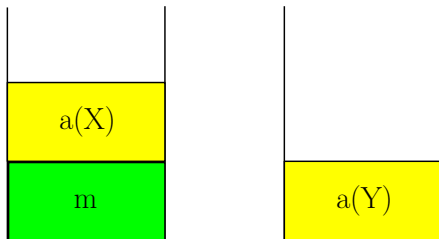
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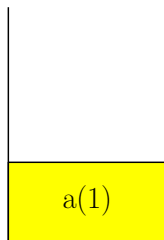
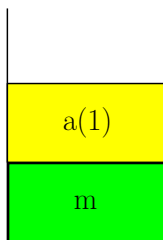


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GOALS



IAP: non-deterministic example

GOALS

```
m :- a(X) & b(Y).
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```
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```
b([1]).
```

```
b([2]).
```



TRAIL



CHOICE



HEAP

IAP: non-deterministic example



GOALS

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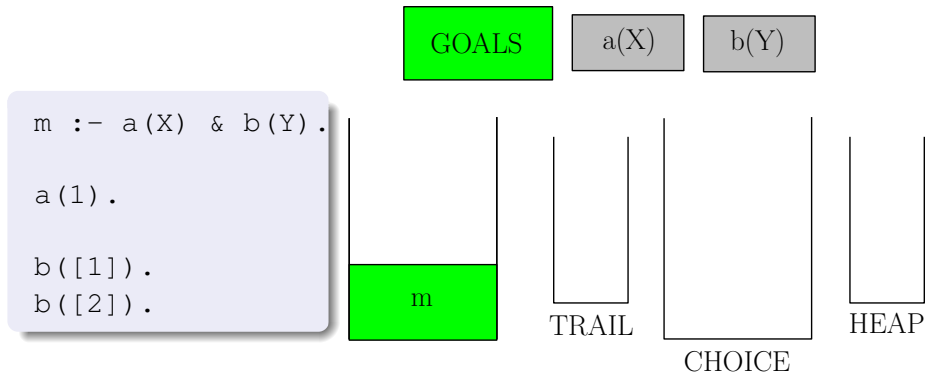
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TRAIL

CHOICE

HEAP

IAP: non-deterministic example



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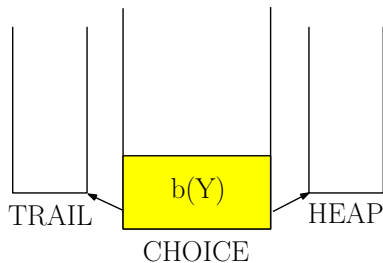
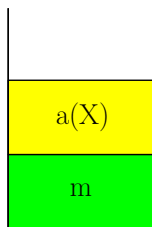
GOALS

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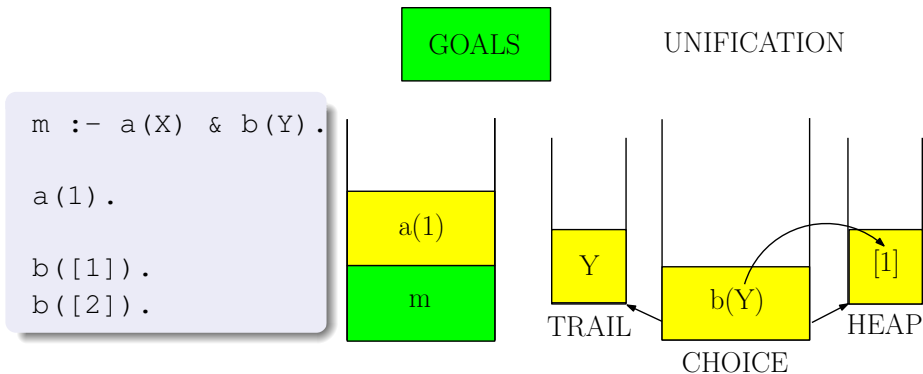
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IAP: non-deterministic example



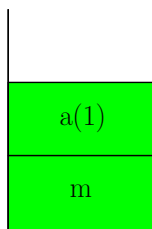
IAP: non-deterministic example

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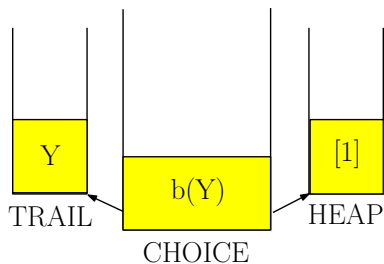
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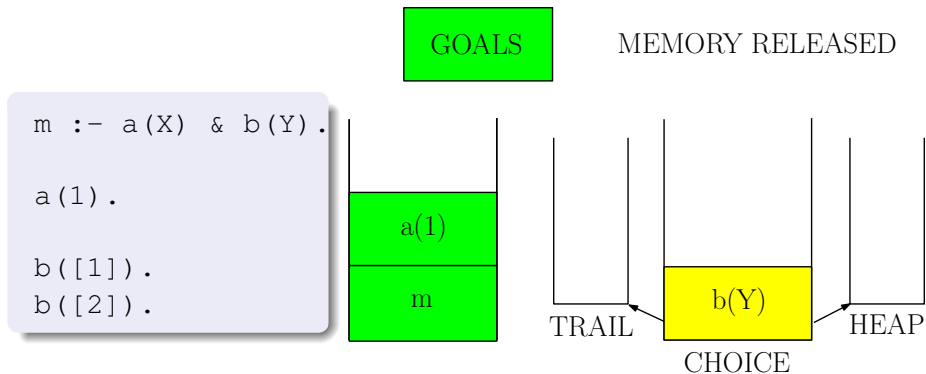
GOALS



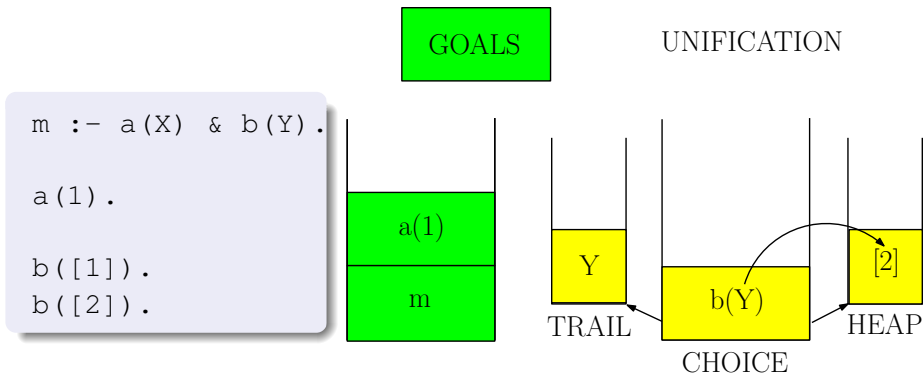
UNTRAILING



IAP: non-deterministic example



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IAP: non-deterministic example

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GOALS



a(1)

m

UNTRAILING



Y

TRAIL

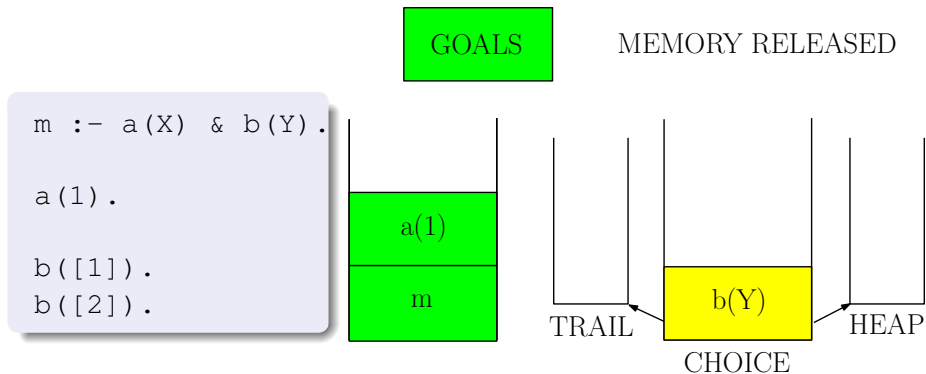
b(Y)

CHOICE

[2]

HEAP

IAP: non-deterministic example



IAP: non-deterministic example with trapped goals

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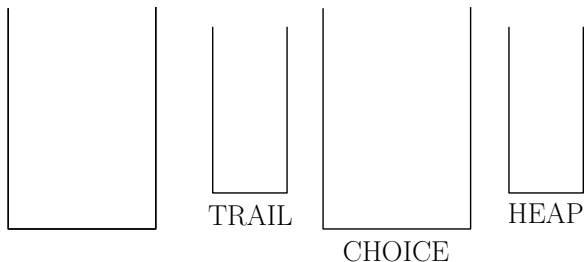
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GOALS



IAP: non-deterministic example with trapped goals

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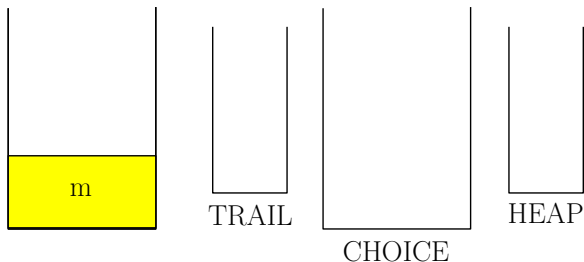
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GOALS

c

b(Z)

m

TRAIL

CHOICE

HEAP

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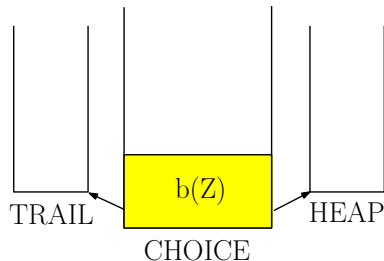
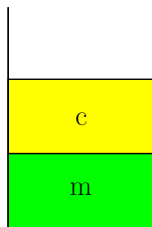
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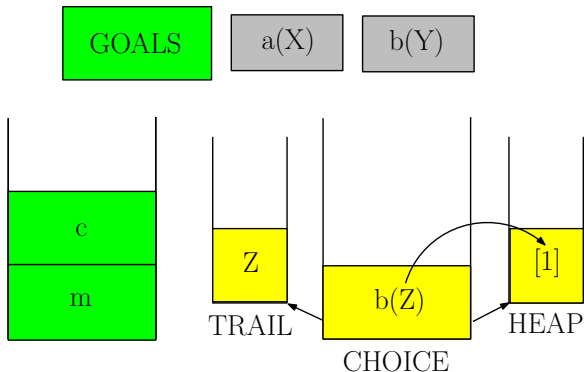
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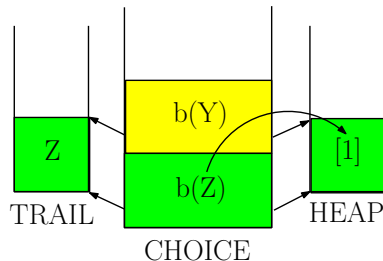
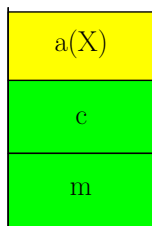
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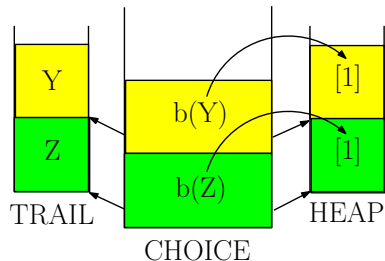
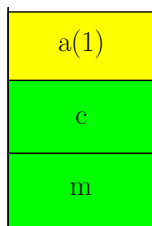
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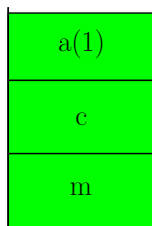
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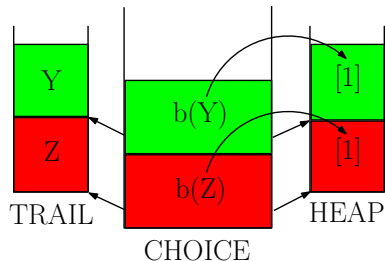
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b([1]).
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GOALS



TRAPPED GOAL!



Solving the trapped goals problem

- Classical approaches:
 - ▶ Implement execution over discontinuous segments.
 - ▶ Avoid trapped goals through scheduling limitations.
- Our proposal: segment-swapping operation.

Dealing with trapped goals: discontiguous execution segments

- Large changes to the WAM implementation \Rightarrow overhead!
- Low-level WAM extensions need to be revisited.
- Difficult maintenance (more complex than the classical one).

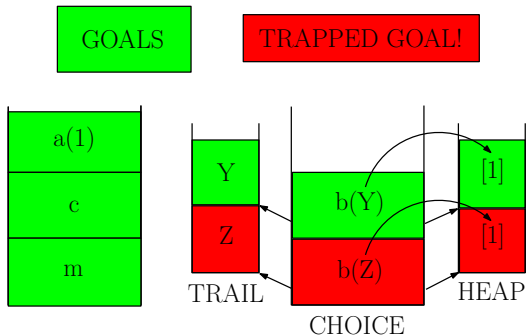
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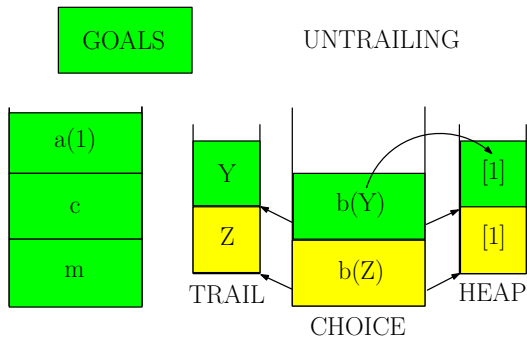
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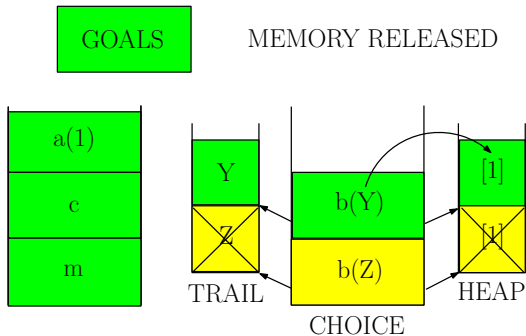
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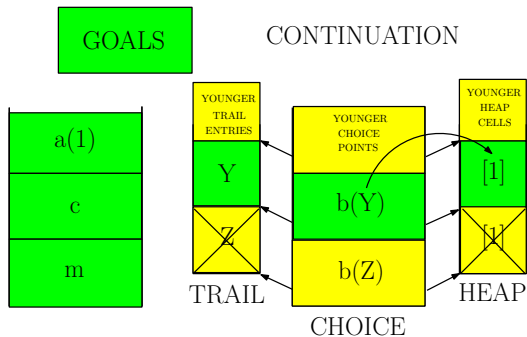
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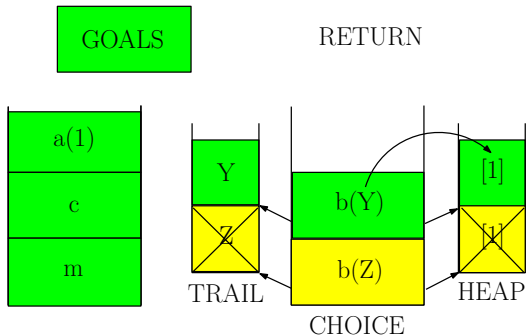
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Dealing with trapped goals: imposing scheduling limitations

- Solution: do not select “older” goals if they will stack over “younger”
 - ▶ Precedence analysis.
 - ★ Goal age: $a(X)$ older than $b(Y)$ older than $b(Z)$.
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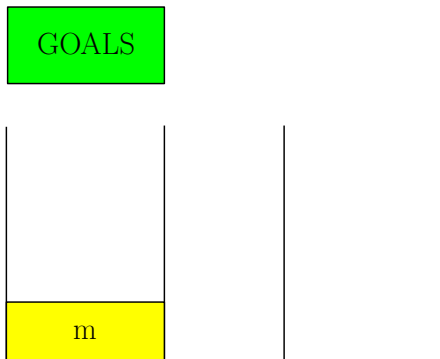
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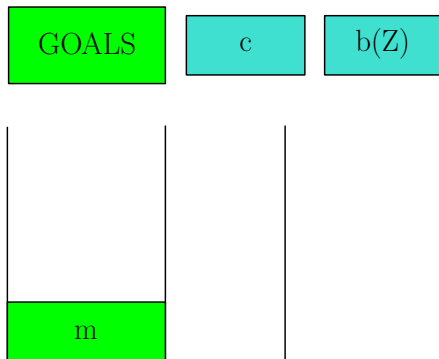
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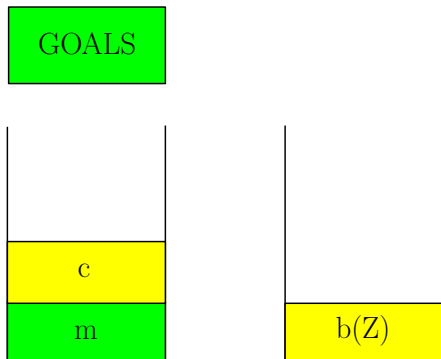
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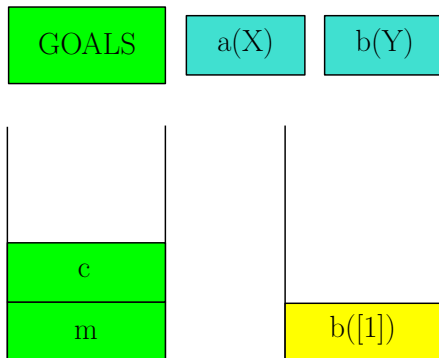
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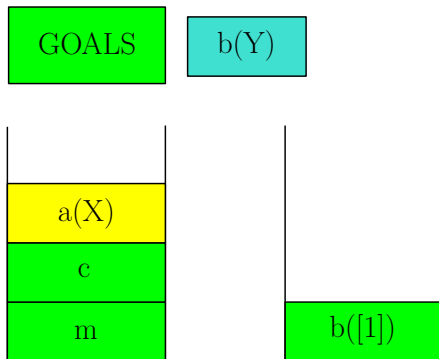
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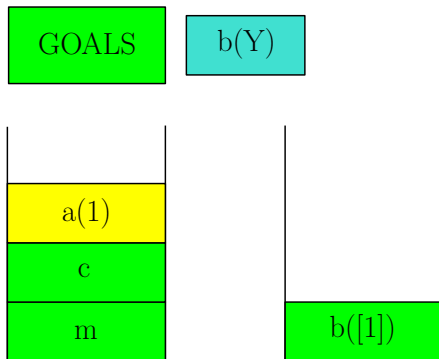
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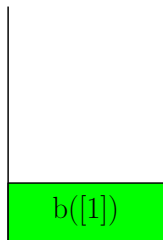
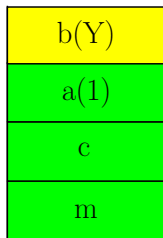
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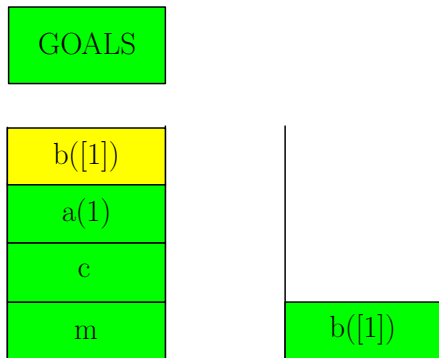
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Dealing with trapped goals (our solution): segment-swapping approach

- Minimal changes to the WAM \Rightarrow sequential execution unaffected.
- Trapped goals allowed \Rightarrow potential parallelism unaffected.
- **Segment-swapping** of trapped goals to recover WAM invariants:
 - ▶ Complex operation, but it is local and modular.

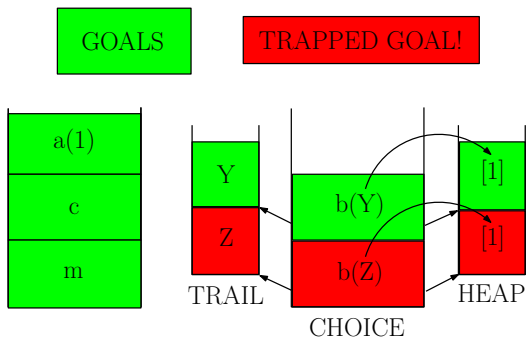
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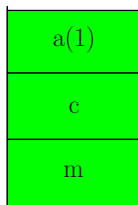
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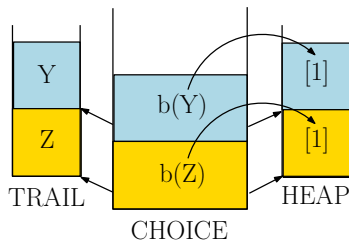
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GOALS



SWAPPING OPERATION



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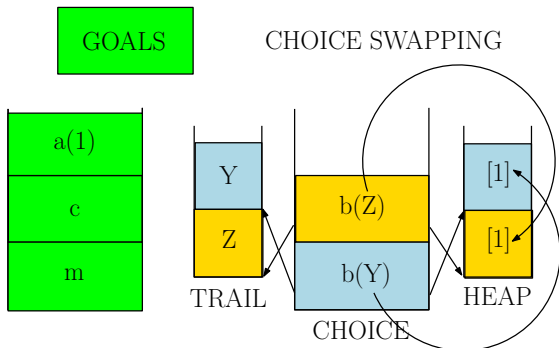
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a(1).
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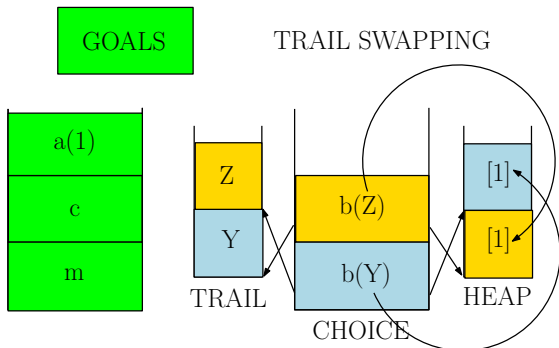
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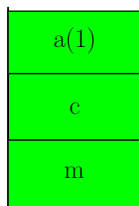
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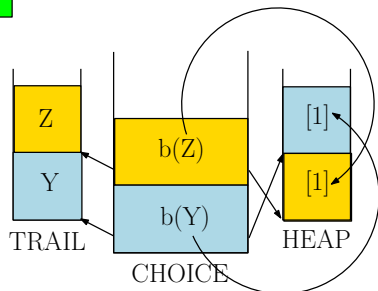
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GOALS



TRAIL_PT UPDATING



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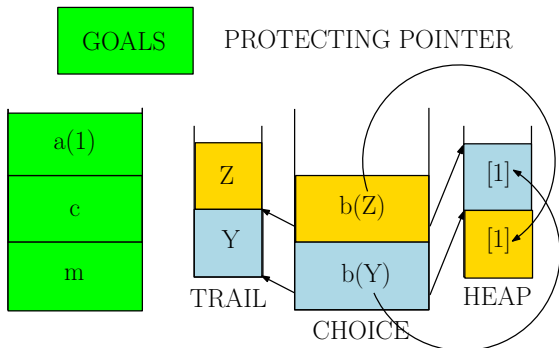
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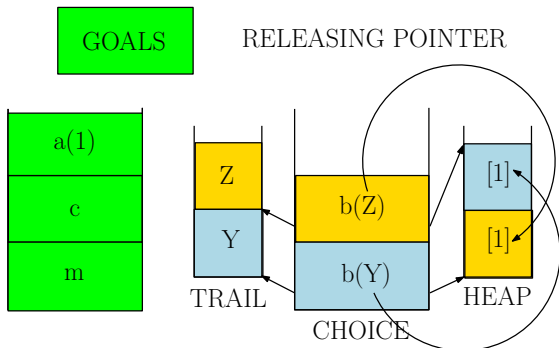
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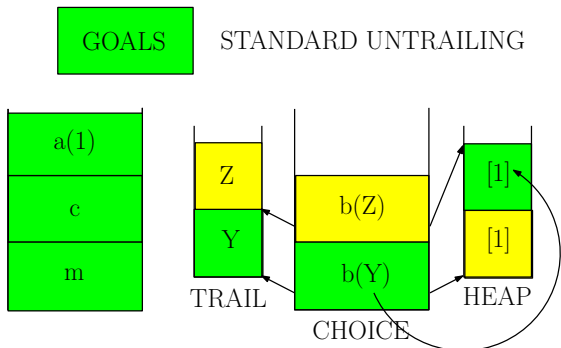
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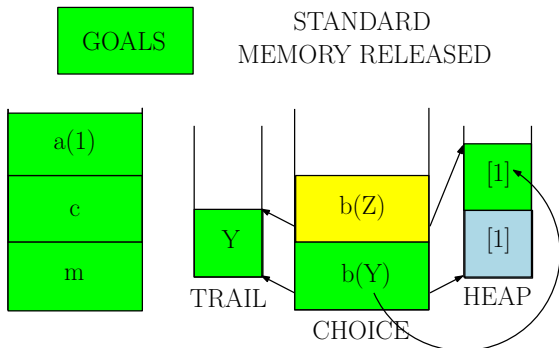
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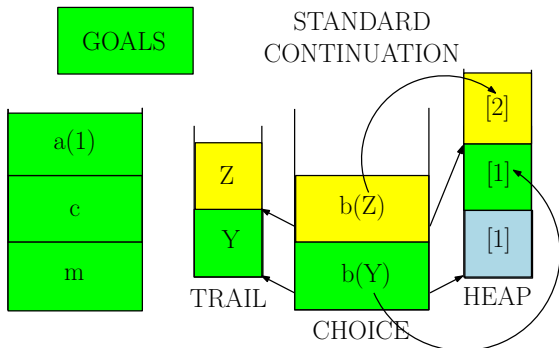
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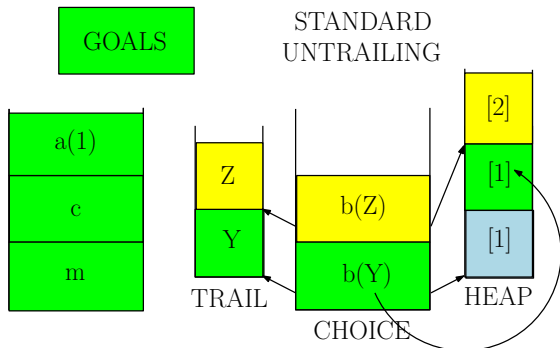
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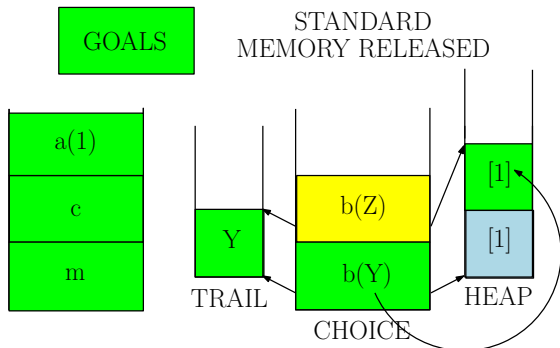
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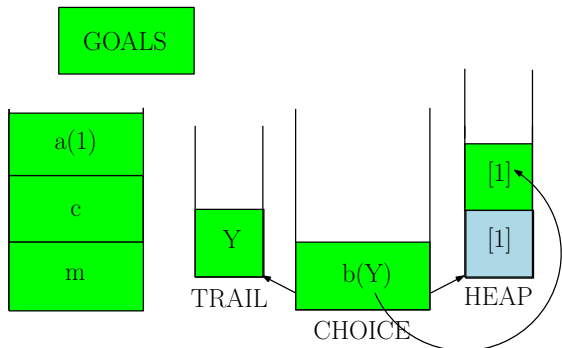
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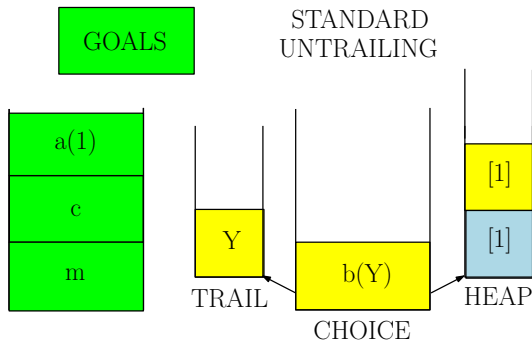
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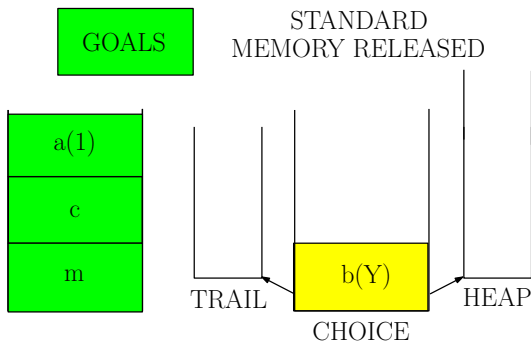
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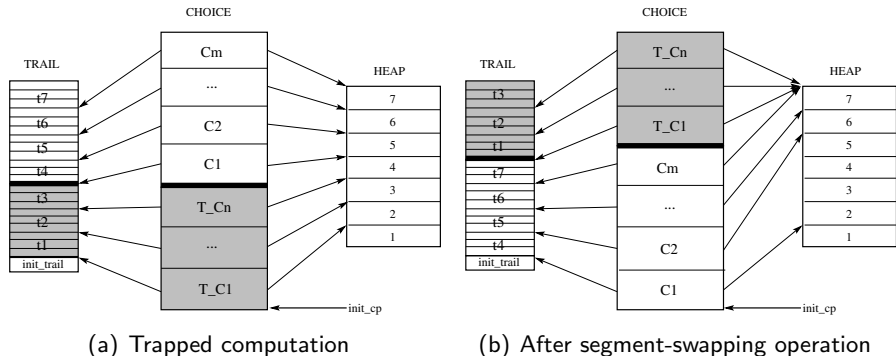
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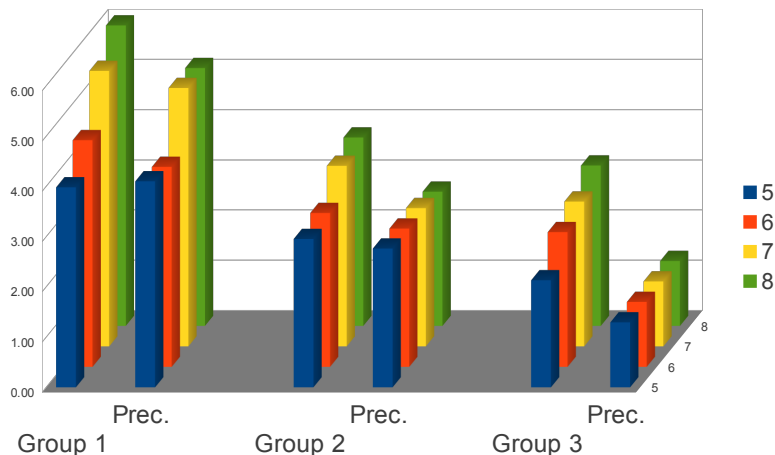


Segment-swapping operation: high level description



Impact of restrictions on precedence

Speedups: swapping vs. precedence



- Precedence restriction limits parallelism and affects performance.

Segment-swapping overhead

	5		6		7		8	
	Freq	Lost	Freq	Lost	Freq	Lost	Freq	Lost
<i>fft</i>	0.05	0.00	0.09	0.00	0.10	0.00	0.15	0.00
<i>fibo</i>	0.03	0.00	0.03	0.01	0.04	0.01	0.06	0.02
<i>han</i>	0.02	0.00	0.02	0.00	0.04	0.00	0.04	0.00
<i>han_dl</i>	0.03	0.05	0.04	0.05	0.03	0.05	0.04	0.07
<i>mmat</i>	0.00	0.00	0.00	0.00	0.02	0.01	0.00	0.00
<i>pal</i>	0.00	0.00	0.02	0.00	0.01	0.00	0.03	0.00
<i>qs</i>	0.07	0.00	0.11	0.00	0.06	0.00	0.09	0.00
<i>qs_dl</i>	0.06	0.00	0.13	0.01	0.11	0.01	0.11	0.01
<i>iqs</i>	0.18	0.02	0.26	0.02	0.27	0.02	0.35	0.03
<i>iqs_dl</i>	0.15	0.02	0.20	0.02	0.28	0.03	0.36	0.03
<i>tak</i>	0.01	0.00	0.13	0.00	0.07	0.00	0.05	0.00
<i>qs_nd</i>	0.14	0.00	0.21	0.00	0.33	0.01	0.39	0.01

- **Freq**: Trapped backtracking fraction vs. total backtrackings.
- **Lost**: Swapping execution time fraction vs. total execution time.

Conclusions

- Previous solutions to trapped goal problem not ideal:
 - ▶ Precedence analysis limits parallelism.
 - ▶ Discontiguous execution segments is very complex.
- We propose segment-swapping approach:
 - ▶ Can be made to not affect sequential execution performance.
 - ▶ Easier to maintain due to its locality and modularity.
 - ▶ Good parallel performance.

Segment-swapping vs. precedence analysis

	5		6		7		8	
	SS	Prec	SS	Prec	SS	Prec	SS	Prec
<i>fft</i>	2.68	2.69	2.87	2.68	2.97	2.67	3.02	2.68
<i>fibo</i>	3.98	4.10	4.51	3.98	5.48	5.14	5.98	5.13
<i>han</i>	3.24	3.24	3.41	3.21	3.74	3.23	4.11	3.42
<i>han_dl</i>	2.95	2.76	3.06	2.75	3.59	2.75	3.75	2.67
<i>mmat</i>	3.72	3.67	4.35	4.11	4.97	4.68	5.63	5.42
<i>pal</i>	3.18	1.82	3.29	3.17	3.60	3.18	3.96	3.03
<i>qs</i>	2.69	2.29	2.84	2.29	3.42	2.29	3.73	2.29
<i>qs_dl</i>	2.65	2.19	3.13	2.19	3.25	2.19	3.32	2.16
<i>iqs</i>	2.27	1.33	2.43	1.33	2.80	1.33	3.02	1.33
<i>iqs_dl</i>	2.13	1.29	2.68	1.29	2.88	1.29	3.19	1.29
<i>tak</i>	3.50	3.50	3.54	3.54	4.47	3.54	4.57	3.74
<i>qs_nd</i>	1.93	1.59	2.01	1.59	2.34	1.59	2.54	1.66

- **SS**: segment-swapping approach.
- **Prec**: scheduling limitation approach.