Computational Logic

Concurrent (Constraint) Logic Programming

Concurrent Logic Programs

- Predicate: Set of clauses
- Clause: $Head : Guard \mid Body$.
 - $\diamond Head$ is an atom
 - $\diamond Guard$ and Body are conjunctions of atoms
- Resolvent: Set of goals (instances of atoms)
- Operational semantics: rewrite a goal in the resolvent with one of the clauses in the matching predicate definition
- Concurrency:
 - "No" goal selection rule (i.e., concurrent selection rule)
 - "No" clause search rule (i.e., concurrent search rule)

Synchronization Rules

- Clause matching: Head + Guard.
 - ♦ Head matches the goal
 - ♦ Guard is successful
- A head matches a goal if the goal is an instance of the head
- A guard is executed in one-way unification mode
- Suspension: if a head does not match the goal, but it could do so in the future, then it *suspends*

An Example

```
p(X):- X = a | r.
p(X):- X = b | s.

q(X):- true | X = b.
?- p(X), q(X).
```

- There is no ordering in the execution of $\langle p(X), q(X) \rangle$
- There is no ordering in the execution of clauses of p(X)
- Clauses of p(X) suspend
- The clause of q(X) continues ("commits")
- Then, q(X) instantiates $\{X/b\}$ in the body
- The second clause of p(X) continues ("commits"), while first clause fails.

Logic vs. Concurrent Logic Programming

• The logical variable as a communication channel

Logic	Concurrent Logic
shared logical variable	communication channel
instantiation	communication
head unification	synchronization

Unification Revisited:

- ♦ One-way (Read-only) unification Ask
 - * in Head and in Guard
- ♦ Two-way (Output) unification Tell
 - * only in Body
- Suspension:
 - * Due to read-only unification in clause selection

Logic vs. Concurrent Logic Programming

- Committed-choice: clause selection is irrevocable
- No backtracking allowed

Logic	Concurrent Logic
cut	commit
"don't know"	("don't care" non-determinism)
non-determinism	indeterminism
search	selection

• Guards:

- ⋄ Flat guards: only selected predicates in guards
 - * (Special) builtins
 - * Possibly also facts
- ♦ Deep guards: calls to any predicate allowed in guards
 - * User-defined predicates, too

Logic vs. Concurrent Logic Programming

Goals as processes:

Logic	Concurrent Logic
atomic goal	process
goal (set of atoms)	process network
clause	process instruction

Process Behaviour:

- Change state of process network:
 - * Become a new process:
 - * Become *k* concurrent processes:
- ♦ Halt:
- Change state of data:
- Some syntactic sugar:

$$\diamond A : G \mid true. \Leftrightarrow A : G \mid .$$

$$\diamond A := true \mid G. \Leftrightarrow A := \mid G. \Leftrightarrow A := G.$$

$$\diamond A : true \mid true. \Leftrightarrow A.$$

$$A : G \mid B$$
.

$$A : G \mid B_1...B_k.$$

$$A := G \mid true.$$

$$A : G \mid ...A.$$

Process Behaviour Examples

• Become a new process: $A : G \mid B$.

$$p(X):-X=f(a,Y) \mid q(Y).$$

• Become k concurrent processes: $A : G \mid B_1...B_k$.

$$p(X) := X = f(A,B,C) \mid q(A), r(B), s(C).$$

• Halt: $A : G \mid$.

$$p(X):-X=f(a)$$
 |.

• Change state of data: $A : G \mid \dots A$.

$$p(X):- X=f(a,Y) \mid Y=f(b,Z), p(Z).$$

 $p(I,S):- I=[H|NI], int(H) \mid NS is S+H, p(NI,NS).$

Incomplete Messages

• Back-communication:

Incomplete Messages (Contd.)

Dialogue:

```
?- q(X), p(more(X)).
p(more(X)):- X=f(a,Y), p(Y).
p(more(X)):- X=f(b,Y), p(Y).
p(ok).

q(f(X,Y)):- X=b | Y=more(Z), q(Z).
q(f(X,Y)):- X=a | Y=ok.
```

Network formation and reconfiguration:

```
?- q(A), p(A).
p(A):- A=channels(X,Y,Z), p1(X), p2(Y), p3(Z).
q(channels(X,Y,Z)):- q1(X), q2(Y), q3(Z).
```

The Logical Variable

- A shared variable acts like:
 - A communication channel to send a message
 - A shared location being accessed concurrently
- Equivalences/conceptual view:
 - One shared variable = One message
 - Instantiation = Sending a message
 - Partially instantiated term = incomplete message = open channel
 - Ground term = complete message = closed channel
 - Recursive term = stream of messages
- Incomplete structures: an incomplete message can be thought of as:
 - A message being incrementally sent
 - An open communication channel
 - A message with sender's identity
 - A structure being co-operatively constructed

Streams of Messages

A stream producer

```
naturals(N,Is):-Is=[N|Is1], N1 is N+1, naturals(N1,Is1).
```

A stream consumer

```
sum([N|Is], Tmp, Sum):-N>=0 | TN is Tmp+N, sum(Is,TN,Sum).
```

Producer/Consumer (asynchronous)

```
?- naturals(0,I), sum(I,0,Total).
```

Producer/Consumer on demand (synchronous)

```
?- naturals(0,I), sum(I,0,Total), I=[_|_].
```

```
naturals(N,[I|Is]):-I=N, N1 is N+1, naturals(N1,Is).
```

```
sum([N|Is],Tmp,Sum):-N>=0 | Is=[_|_], TN is Tmp+N, sum(Is,TN,Sum).
```

Key issue: who produces the buffer?

Merging and Dispatching Streams

A stream merger:

```
merge([X|Xs],Ys,Out):- Out=[X|Zs], merge(Xs,Ys,Zs).
merge(Xs,[Y|Ys],Out):- Out=[Y|Zs], merge(Xs,Ys,Zs).
merge([],Ys,Out):- Out=Ys.
merge(Xs,[],Out):- Out=Xs.
```

A (copying) stream dispatcher?

```
dispatch([X|Xs],Out1,Out2):- Out1=[X|Ys], Out2=[X|Zs], dispatch(Xs,Ys
dispatch([],Out1,Out2):- Out1=[], Out2=[].
```

• A (caotic) stream dispatcher:

```
dispatch([X|Xs],Out1,Out2):- Out1=[X|Ys], dispatch(Xs,Ys,Out2).
dispatch([X|Xs],Out1,Out2):- Out2=[X|Ys], dispatch(Xs,Out1,Ys).
dispatch([],Out1,Out2):- Out1=[], Out2=[].
```

• A stream dispatcher with senders' identities

```
dispatch([mess(1,X)|Xs],Out1,Out2):- Out1=[X|Ys], dispatch(Xs,Ys,Out2)
dispatch([mess(2,X)|Xs],Out1,Out2):- Out2=[X|Ys], dispatch(Xs,Out1,Ys)
dispatch([],Out1,Out2):- Out1=[], Out2=[].
```

Fairness

"An event that may occur will eventually occur"

- Or-Indeterminism: clause selection ⇒ Or-Fairness (clauses eventually selected)
- And-Indeterm.: goal reduction ⇒ And-Fairness (allows non-terminating procs.)
- A stream merger:

```
merge([X|Xs],Ys,Out):- Out=[X|Zs], merge(Xs,Ys,Zs).
merge(Xs,[Y|Ys],Out):- Out=[Y|Zs], merge(Xs,Ys,Zs).
merge([],Ys,Out):- Out=Ys.
merge(Xs,[],Out):- Out=Xs.
```

Key: or-fairness required, otherwise it is just append!

An eager producer:

```
naturals(N,Is):- \mid Is=[N|Is1], \ N1 \ is \ N+1, \ naturals(N1,Is1). ?- naturals(0,I), \ sum(I,0,Total).
```

Key: and-fairness required, otherwise nothing is ever consumed!

Termination Issues

Non-terminating (but running) processes:

```
?- naturals(I), sum(I,Total), I=[_|_].
naturals(I):- naturals(0,I).
naturals(N,[I|Is]):- | I=N, N1 is N+1, naturals(N1,Is).
sum(I,Total):- sum(I,0,Total).
sum([N|Is],Tmp,Sum):- N>=0 | Is=[_|_], TN is Tmp+N, sum(Is,TN,Sum).
```

Termination Issues (Contd.)

Deadlock:

```
?- q(X), p(X).
p(more(X)):- X=f(a,Y), p(Y).
p(more(X)):- X=f(b,Y), p(Y).
p(ok).

q(f(X,Y)):- X=b | Y=more(Z), q(Z).
q(f(X,Y)):- X=a | Y=ok.
```

Bounded-Size Communication Media

 Producer/Consumer with fixed sized communication (e.g., size=4) and termination:

```
?- naturals(0,I), sum(I,0,Total), I=[_1,_2,_3,_4].
naturals(N,[I|Is]):- | I=N, N1 is N+1, naturals(N1,Is).
naturals(N,[]).
sum([N|Is],Tmp,Sum):- N>=0 | TN is Tmp+N,sum(Is,TN,Sum).
sum([],Tmp,Sum):- | Sum=Tmp.
```

Key: the communication media is produced from outside and fixed size!

Dynamically-sized media:

```
?- naturals(0,I), sum(I,0,Total), medium(4,I).
medium(0,Stream) :- Stream = [].
medium(N,Stream):- N>0 |Stream=[_|Stream1], medium(N-1,Stream1).
```

Bounded-Buffer Communication

Bounded buffer:

```
buffer(0,Stream,Tail):- Stream=Tail.
buffer(N,Stream,Tail):- N>0 | Stream=[_|Stream1], buffer(N-1,Stream1,Tail):- N>0 | Stream=[_|Stream1]
Creates buffer as open list of N elements, passes handle to list end
```

Simple producer with termination at Max elements:

```
naturals(N,[I|Is],Max):- N<=Max \mid I=N, N1 is N+1, naturals(N1,Is,Max). \\ naturals(N,I,Max):- N>Max \mid I=[].
```

Suspended until buffer available. Closes buffer at Max elements

Consumer:

Suspended until buffer and element available. Adds one more element to the buffer for each element consumed.

Usage (e.g., for buffer length = 18, termination at 1000 elements):
 ?- naturals(0,Buffer,1000), sum(Buffer,Tail,0,Total), buffer(18,Buffer,Tail,0)

Bounded-Buffer Communication (Contd.)

- Overall effect is still asynchronous!
- Producer can get ahead of consumer by a fixed number of elements. After that, suspended on stream until Consumer requests more.

Streams of Messages: Protocols

- One-to-one communication:
 One producer + One consumer
- Duplex communication:
 Two producer/consumers
- Broadcast communication:
 One producer + Many consumers
- Many-to-one communication:
 Many producers + One consumer
- Blackboard communication:
 Many producers + Many consumers:
 Many producers/consumers

Broadcast Communication

Matrix multiplication:

- Broadcasting of V to all vv/3 processes
- Dynamically configured network of vv/3 processes

Many-to-one Communication

• A data abstraction: queues

Many-to-one Communication (Contd.)

A simulator of a multiprocessor machine

```
?- processors(10, Job), Job=...
processors(N,X):-
     queue(S,[X|Xs],Xs),
     processors(1,N,S).
processors(N,N,S):-
     processor(N,idle,S).
processors(N1,N4,S):-
         is (N1+N4)/2 \mid N3 is N2+1.
     processors(N1,N2,S1),
     processors(N3,N4,S2),
     merge(S1,S2,S).
```

- N processor/3 proc. communicating with one queue/3 proc.
- Statically configured network of proc.: spawning / computing phases ("systolic")

Many-to-many Communication

A network of producers and consumers

```
?- consumers(Buffer), producers(Buffer).
producers(Stream):- p1(X), p2(Y), p3(Z),
     merge(X,Y,Stream1), merge(Z,Stream1,Stream).
consumers(Stream): - c1(Stream), c2(Stream), c3(Stream).
p1(S):- S=[message(1,Mess)|Xs], produce(Mess), p1(Xs).
\mathfrak{p}1(S):-S=[].
c1([X|Xs]):-X=message(1,Mess) \mid consume(Mess), c1(Xs).
c1([X|Xs]):- X=message(Id,Mess), Id=\=1 | c1(Xs).
c1(\lceil \rceil).
```

- Blackboard Communication:
 - ♦ Needed driver for the blackboard

Operational Semantics

Rewriting system

$$match(A,A') = \begin{cases} \theta & \text{if } A = A'\theta \ mgu(A,A') = \theta \\ fail & \text{if } mgu(A,A') = fail \\ suspend & \text{otherwise} \end{cases}$$

$$try(A,(A' \leftarrow G \mid B)) = \begin{cases} \theta & \text{if } match(A,A') = \theta \land \\ check(G\theta) = true \\ fail & \text{if } match(A,A') = \theta \land \\ check(G\theta) = fail \lor \\ match(A,A') = fail \\ suspend & \text{otherwise} \end{cases}$$

Operational Semantics (Contd.)

- Reduction: $A_1...A_n$; $\theta \to (A_1...B_1...B_k...A_n)\theta'$; $\theta \circ \theta'$ if $\exists C = A \leftarrow G \mid B_1...B_n$ s.t. $try(A_i, C) = \theta'$
- Failure: $A_1...A_i...A_n$; $\theta \to fail$; θ if $\forall C \ try(A_i, C) = fail$
- Guard checking:
 - ♦ Flat guards: use match in all unifications
 - Deep guards: copy environment

(Some) Concurrent Logic Languages

- Parlog [Clark, Gregory 83]
 - mode declarations for input/output arguments
 - safe clauses: output instantiation in guards is an error
 - one-way unification in guards
- Concurrent Prolog [Shapiro 84]
 - read-only annotation of variables in calls
 - local environments for guards
 - atomic extended head unification
- GHC (Guarded Horn Clauses) [Ueda 85]
 - different interpretation of unification in guard and body
 - suspension on output instantiation in guards
 - general unification with guard restriction

(Some) Concurrent Logic Languages (Contd.)

- Implementation Issues:
 - Parlog
 - * compile-time safety check
 - Concurrent Prolog
 - * support for local environments
 - * detection of inconsistency with global environment
 - ♦ GHC
 - * identification of variables on which to suspend
- Problems: no backtracking.
- More Recent Systems:
 - Andorra-I: only deterministic computations proceed.
 - AKL: goals execute in a local environment.
 - BinProlog: communication through blackboard.
 - CIAO: communication through shared database.