Abstract Program Slicing

Damiano Zanardini

CLIP, Universidad Politécnica de Madrid

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Overview

An intuition

some basic ideas taken from published (to appear) work [SCAM'08]

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a brief discussion on practicality, usefulness, etc.

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After all, it's a workshop

future work, extensions, ideas

Introduction

Program slicing: $\mathcal{P}^S$ is the slice of $\mathcal{P}$ with respect to the criterion S

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Observations

- S (the value of a set of vars) can be too restrictive, since the interest may be on some *data property* (e.g., the *nullity* of references)
- slices are sometimes too big for practical use (*debugging*, *program understanding*)
- dealing with properties *relaxes* the notion of dependency (abstract dependency, ANI, etc.)

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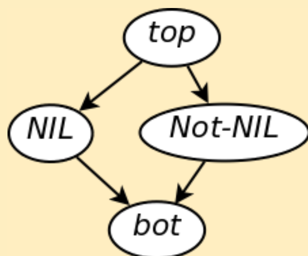
Slicing at the abstract level

might be successful in modelling interesting tasks and, at the same time, obtaining smaller slices

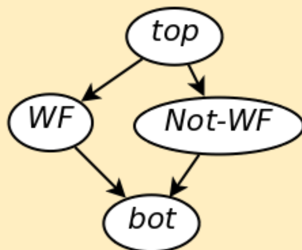
An example [SCAM'08]

Well-formed lists: $\langle 1, 2, 3, 4, [0]\rangle {+}{+} \langle 5, 6, [0]\rangle = \langle 1, 2, 3, 4, 5, 6, [0]\rangle$

the properties of interested are represented by abstract domains for *nullity* and *well-formedness*:



ρ_{nil}



ρ_{WF}

$$wellFormed(x) \equiv notNil(x) \wedge lastEl(x).data = 0$$

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Append-reverse: $\langle 1,2,3,4,[0]\rangle {+}{+} \langle 5,6,[0]\rangle = \langle 4,3,2,1,5,6,[0]\rangle$

$$
\begin{array}{l}
\mathit{list}1 \;:=\; a_1;\\
\mathit{list}2 \;:=\; a_2;\\
\textbf{while}\ (\mathit{notLast}(\mathit{list}1))\ \{\\
\quad \mathit{tmp} \;:=\; \mathit{list}1.\mathit{next};\\
\quad \mathit{list}1.\mathit{next} \;:=\; \mathit{list}2;\\
\quad \mathit{list}2 \;:=\; \mathit{list}1;\\
\quad \mathit{list}1 \;:=\; \mathit{tmp};\\
\}\\
\textbf{if}\ (\mathit{nil}(\mathit{list}2) \ \vee\ \mathit{illFormed}(\mathit{list}2))\ \{\\
\quad \mathit{res} \;:=\; \mathit{nil}\ \}\ \textbf{else}\ \{\ \mathit{res} \;:=\; \mathit{list}2\ \}
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list2 := a2;
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if (nil(list2) ∨ illFormed(list2)) {
  res := nil } else { res := list2 }
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Code	
$list1 \; := \; a_1;$	any
$list2 \; := \; a_2;$	$\mathcal{A}_{\rho_{\mathrm{WF}}}(list2)$
while $(notLast(list1))$ $\{$	
$\quad tmp \; := \; list1.next;$	
$\quad list1.next \; := \; list2;$	$\ldots$
$\quad list2 \; := \; list1;$	
$\quad list1 \; := \; tmp;$	
$\}$	$\mathcal{A}_{\rho_{\mathrm{WF}}}(list2)$
if $(nil(list2) \; \vee \; illFormed(list2))$ $\{$	
$\quad res \; := \; nil$ $\}$ **else** $\{$ $res \; := \; list2$ $\}$	$\mathcal{A}_{\rho_{nil}}(res)$

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if $(nil(list2) \; \vee \; illFormed(list2)) \; \{$
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Basic ideas

When a command can be removed

- it *preserves* some *property* (as $x := x + 2$ preserves the *parity* of x)
- such property was obtained by *propagating* the slicing criterion backwards *from the end of the program* (WLOG) (e.g., in the example, the final nullity of *res* is propagated backwards to the well-formedness of *list2*)

A semantic characterization of these requirements can be given

Basic ideas

Abstract semantics and slicing criteria

- an abstract semantics $[\![ ]\!]^{\#}_S$ is *induced* by the slicing criterion S, which specifies the property to be preserved by the slicing

$$\forall \sigma.\ [\![P]\!]^{\#}_S(\sigma) = [\![P^S]\!]^{\#}_S(\sigma)$$

- criterions are expressed as *agreements* between two states: $\mathcal{A}(\sigma_1, \sigma_2)$ means that both states behave the same w.r.t. the abstract property specified by $\mathcal{A}$
- S requires the output of the program and of the slice to agree on $\mathcal{A}$:

$$\mathcal{A}\left([\![\mathcal{P}]\!](\sigma), [\![\mathcal{P}^S]\!](\sigma)\right)$$

Which kind of machinery is needed, in practice

- a way to compute when a command does not make a difference (is *invariant*) on the abstract property

$$\mathcal{A}(\llbracket C \rrbracket(\sigma),\ \sigma)$$

  saying that $\mathcal{A}$ is invariant on C means that C cannot be distinguisehd from *skip* as regards the property of interest
- the computation of such results must be *sound*, i.e., the invariance must be *guaranteed*

Basic ideas

Which kind of machinery is needed, in practice

- how criteria (properties) are propagated backwards through the code, i.e., given $\mathcal{A}'$ after C, find the best $\mathcal{A}$ before C such that

$$\forall \sigma_1, \sigma_2. \quad \mathcal{A}(\sigma_1, \sigma_2) \;\Rightarrow\; \mathcal{A}'(\llbracket C \rrbracket(\sigma_1), \llbracket C \rrbracket(\sigma_2))$$

- these are example (Hoare-like) *rules* for propagating agreements through a program

$$\frac{\{\mathcal{A}\}\ C\ \{\mathcal{A}'\} \quad \{\mathcal{A}'\}\ C'\ \{\mathcal{A}''\}}{\{\mathcal{A}\}\ C\ ;\ C'\ \{\mathcal{A}''\}}\ \text{A-CONCAT}$$

$$\frac{\{\mathcal{A} \sqcap \mathcal{A}_b\}\ C_w\ \{\mathcal{A} \sqcap \mathcal{A}_b\}}{\{\mathcal{A} \sqcap \mathcal{A}_b\}\ \mathit{while}\ (b)\ \mathit{do}\ C_w\ \{\mathcal{A} \sqcap \mathcal{A}_b\}}\ \text{A-WHILE}$$

Basic ideas

Which kind of machinery is needed, in practice

- when a piece of data *depends* on other data at the abstract level
  - to track the flow of information in the case of *assignments*
  - *syntax* is not enough, not even a reasonable approximation: the difference between *concrete* and *abstract* lies in the *semantics*
  - e.g., the sign of xy^2 only depends on x
- in this direction:
  - *binary* domains (null/non-null, zero/non-zero, etc.)?
  - in this case, *independence* of (a property of) an expression from (a property of) a variable means that knowing the answer to *questions* about x is not needed to answer about the result
  - e.g., if answering to *is x null?* is irrelevant to the question *is e positive?*, then the sign of e does not depend on the nullity of x
  - using BDDs would be practical?

Trying to think general

What we have

the presented version of slicing reasons about abstractions (properties) of the (final) value of variables

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What we (fore)see

yet, what if *non-denotational* information is included in the abstraction?

- e.g., suppose $[\![]\!]^{\#}_{S}$ be an abstraction of the *trace semantics*
- this may allow to reason about the *history* of the computation

Preserving program properties

Possibilities

this approach could possibly allow reasoning about complex, functional properties of a program

- *termination*: $\mathcal{P}^S$ {must|can|cannot} terminate iff $\mathcal{P}$ {must|can|cannot} terminate
- *information flow*: x {must|can|cannot} flow to y in $\mathcal{P}^S$ iff it {must|can|cannot} flow to y in $\mathcal{P}$

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A general framework

- in all cases, the problem is to compute invariance, to propagate properties, to deal with abstract dependence
- clearly, formalizing and manipulating the property of interest can be quite tricky

Preserving program properties

An example

suppose h *cannot* flow to l while l'' *must* flow to l

$$l := h + l''$$

...

$$\textit{if}\ (b)\ \{\ l := l' + 1\ \}\ \textit{else}\ \{\ l := l' + l''\ \}$$

...

- in this case, removing the conditional would break the first requirement, since there *could* be a flow from h to l
- of course, the absence of *must-flow* requirements would imply that the empty program is always a correct slice (unless *self-flows* are forbidden)

Related work

To be completed...

- ANI (Giacobazzi & Mastroeni)
- abstract dependencies (Rival, Mastroeni & Zanardini)
- symbolic execution (King)
- conditioned slicing (Canfora et al.)
- logic for information flow (Amtoft & Banerjee)
- *invariance on commands*?
- ...

References

MZ08

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D. Zanardini. **The Semantics of Abstract Program Slicing**. In *Proc. International Working Conference on Source Code Analysis and Manipulation (SCAM)*, 2008. To appear.